

from a commercial perspective, they can reduce social costs and potential liability risks, thereby improving competitiveness. With the further promotion of ecological civilization construction and the continuous improvement of the ecological life quality of social subjects, the demand of social subjects for ecological products has gradually changed from basic and simple to complex and diverse [11]. On the basis of deepening the market-oriented reform of ecological products, we define ecological products as products that have undergone strict ecological design, typically through ecological identification, ecological diagnosis, ecological definition, and ecological evaluation, followed by recurring and optimized adjustment, considering the environmental impact of the entire process of the product lifecycle. The positive externalities of ecological products in the environment are reflected in the improvement of the ecosystem, from the acquisition of raw materials to product production, consumer use, and ultimately recycling. Therefore, we believe that ecological products not only refer to traditional biomass supplies such as water, wood, and air, but also include goods and services provided by humans, such as new energy, physical carbon sequestration, and soil purification. However, when ecological products play an external role, there are still issues such as the absence of laws and regulations or mandatory policies, unclear market establishment and trading rules, and market supervision failure. A closed-loop mechanism for ecological product consumption should be established.

Traditionally, it is believed that the price of a product reflects consumers' willingness to consume from three different perspectives. First, numerous studies suggest that consumer willingness is affected by demographic and economic variables [12–15]; the second is to consider information and knowledge on environmental issues [16, 17]; the third view adopts psychological variables, including values, lifestyles, personality characteristics, and attitudes [18–21]. The purpose of this study is to reflect different environmental protection concepts through consumer choices of general products and ecological products, which is reflected in the utility function as the negative externality of general products and the positive externality of ecological products.

To take "ecological products" into consideration in an economic sense is to seek the path of product marketization from the perspective of balanced production and demand. The most basic and effective regulatory mechanism for the marketization of ecological products is price. Price decision-making refers to the process in which enterprises choose and optimize their product pricing schemes according to their own conditions and market environment. Hermann [22] proposed a dynamic model of price elasticity related to the brand life cycle. Rao & Shakun [23] put forward a price model for new brands to enter the market, which fully considered the market structure, as well as an enterprise's brand prospect and competition goal in the process of realizing the pricing strategy. Dolan & Jeuland [24] built an optimal price model that takes cost dynamics and diffusion process

dynamics into account. However, the connection between supply and demand is the core factor influencing the price formation of any market-oriented product; therefore, we must simultaneously consider the maximization of consumer utility and the maximization of producer profits. The correlation between consumers' ability to pay for ecological products and social demand is positive; that is, consumers' willingness to pay for products is strongly related to production costs. Yang et al. [25], Sun et al. [26], and Wang et al. [27] have conducted different studies in innovation cost reduction, green lending, dual supply-chain pricing, and other fields. Numerous scholars have discussed product pricing using game models [28–30]. Sun and Nie [31] and Huang et al. [32] also presented different forms of the equilibrium solution of a dynamic game. In view of this, we will continue to use the game model to study the pricing behavior of ecological products, mainly setting up a complete-information static game and two complete-information dynamic games between two producers, in which one is a general firm, whose general products have a certain negative externality without considering the impact on the environment, such as fossil energy technology and mining services. Conversely, another is an ecological firm, which produces ecological products with positive externalities, such as new energy technologies and soil purification services.

Furthermore, market competition is inseparable from the government's economic control policies, and the commonly used tools are taxes and subsidies. Producers' profits are largely determined by taxes/subsidies. Levying environmental protection taxes on output can significantly improve consumption structure and ecology [33–35]. Krass et al. [36] established a price-dependent demand model, focusing on the role of environmental taxes in reducing environmental pollution. Yang et al. [37] studied the impact of a renewable energy subsidy game on social welfare based on a dynamic equilibrium model. The level of subsidies greatly affects producers' production and pricing decisions [38, 39]. Gouda et al. [40] and Bian & Zhao [41] considered two sets of policy tools and compared the impact of unified subsidy policy and discriminatory subsidy policy on total welfare and the average environment. Ensure fairness and efficiency in resource allocation and environmental protection by utilizing an adjustable combination of tax and subsidy policies [41–43]. Similarly, Zhang et al. [44] introduced the Stackelberg model to study the choice of tax policy, subsidy policy, and tax subsidy policy. Different from the above study, we considered how the benefits of ecological products in different tax and subsidy scenarios affect price. We also explored whether changes in a tax/subsidy can improve market competition as expected by policymakers and urge manufacturers to change their strategies.

Many studies have analyzed ecosystem products and values, promoting research progress in this field. However, existing research has rarely explored the economic value of ecological products, as it is widely believed that ecological products are an ecological concept and have not been considered in the relationship

between production and nature. In addition, in some research on product pricing, apart from focusing on the most important supply-demand relationship, there are few direct considerations of both tax and subsidy effects. This paper emphasizes the tangible economic value of ecological products, which can be reflected in their price formation through supply and demand relationships and tax/subsidy effects. This will provide a new analytical paradigm for the marketization of ecological products.

In summary, the most critical core influencing factor for the formation of ecological product prices is the relationship between supply and demand. By setting the consumption utility function of general products and ecological products, combined with the producer profit function and the equilibrium solution under the duopoly game, we can capture the positive externalities of ecological products and how government taxes/subsidies affect the pricing of ecological products through numerical simulation. The research results will depict the optimization space for price determination in the current market-oriented reform of ecological products, providing a scientific theoretical basis for the marketization of ecological products and also clarifying the direction of government tax/subsidy policy selection, providing scientific guidance for the construction of ecological civilization.

The rest of this paper is organized as follows. The model, based on consumers' heterogeneous preferences and producers' pricing strategies, is presented in methodology section. Subsequently, the game model is analyzed in theoretical analysis and model solution section, and negative and positive externalities are captured. Results and discussion section reports the main results of tax effects and subsidy effects. Concluding remarks are presented in the last section.

Methodology

Consider an industry with two producers producing homogenous products, in which one is a general firm and the other is an ecological firm. The products offered by the general firm have certain negative externalities. On the contrary, ecological products can generate positive externalities. Denote the two producers as G and E , where firm G is a general firm and firm E is an ecological one. We then establish two game models and diverse scenarios of tax and subsidy policies.

Demand Function

p_G is the price of general products, p_E is the price of ecological products, and the quantity of products is q_G and q_E . The utility function of representative consumers is given by:

$$U(p_G, q_G, p_E, q_E, \gamma) = A(q_G + q_E) - \frac{1}{2}(q_G^2 + q_E^2) - \tau q_G - p_G q_G - p_E q_E + \gamma q_G q_E \quad (1)$$

where $A > 0$ is the reserve price (expected expenditure) of the commodity purchased by consumers, $\tau > 0$ is the ecological footprint of general product consumption (negative externality), and γ is the alternativeness when choosing between two commodities, which is the performance of consumers' ecological attitude. Regarding preference (γ is a random variable, $\gamma \in [0, 1]$, $\int_0^1 f(\gamma) d\gamma = 1$), when $\gamma = 0$, consumers have no sense of ecosystem conservation, and $\gamma = 1$ means that consumers strongly support environmental policies and prefer ecological products.

For two products in a market, consumers determine the optimal purchase quantity according to the principle of maximizing their own utility. The inverse demand function is given as follows:

$$\begin{aligned} p_G &= A - q_G - \tau + \gamma q_E \\ p_E &= A - q_E + \gamma q_G \end{aligned} \quad (2)$$

Production Function

The profit functions of firms producing general and ecological products can be expressed as:

$$\begin{aligned} \pi_G &= p_G q_G - c_G q_G - \alpha q_G \\ \pi_E &= p_E q_E - c_E q_E + \beta q_E \end{aligned} \quad (3)$$

For simplification, we introduce the assumption that $c_G < c_E$, implying that the marginal costs of ecological firms are greater than those of general firms. $\alpha > 0$ is the tax on general products, and $\beta > 0$ is the subsidy on ecological products.

Theoretical Analysis and Model Solution

In this section, the above model is analyzed using a static game and two dynamic games of complete information between a general firm and an ecological firm. Here, we capture the positive/negative externalities by comparing product prices with producers' profits.

Static Game of Complete Information

In a similar product market, both firms compete in output, take actions according to their competitors' strategies, and assume that their competitors continue to do so, so as to make their own decisions. The first-order optimal conditions for the profit maximization of two firms can be obtained from Eq. (3).

$$\begin{aligned} \frac{\partial \pi_G}{\partial q_G} &= A - 2q_G - \tau + \gamma q_E - c_G - \alpha = 0 \\ \frac{\partial \pi_E}{\partial q_E} &= A - 2q_E + \gamma q_G - c_E + \beta = 0 \end{aligned} \quad (4)$$

$$\begin{aligned} q_G &= \frac{A + \gamma q_E - \tau - c_G - \alpha}{2} \\ q_E &= \frac{A + \gamma q_G - c_E + \beta}{2} \end{aligned} \quad (5)$$

The equilibrium output of two firms under a static game of complete information is:

$$\begin{aligned} q_G^{*,1} &= \frac{(2+\gamma)A - 2(c_G + \alpha + \tau) - \gamma(c_E - \beta)}{4 - \gamma^2} \\ q_E^{*,1} &= \frac{(2+\gamma)A - \gamma(c_G + \alpha + \tau) - 2(c_E - \beta)}{4 - \gamma^2} \end{aligned} \quad (6)$$

By substituting Eq. (6) into Eq. (2), we can obtain the equilibrium prices of the two products as follows:

$$\begin{aligned} p_G^{*,1} &= \frac{(2+\gamma)A + (2-\gamma^2)(c_G + \alpha + \tau) - \gamma(c_E - \beta)}{4 - \gamma^2} - \tau \\ p_E^{*,1} &= \frac{(2+\gamma)A - \gamma(c_G + \alpha + \tau) + (2-\gamma^2)(c_E - \beta)}{4 - \gamma^2} \end{aligned} \quad (7)$$

and

$$\begin{aligned} \frac{\partial p_G^{*,1}}{\partial \gamma} &= \frac{(4 + \gamma^2)(A - c_E + \beta) + 4\gamma(A - c_G - \alpha - \tau)}{(4 - \gamma^2)^2} > 0 \\ \frac{\partial p_E^{*,1}}{\partial \gamma} &= \frac{(4 + \gamma^2 + 4\gamma)A - (4 - \gamma^2 + \gamma)(c_G + \alpha + \tau) - 4\gamma(c_E - \beta)}{(4 - \gamma^2)^2} > 0 \end{aligned} \quad (8)$$

Proposition 1. Under the most ideal premise, $\tau = 0$, $\gamma = 1$, indicating that the initial environmental conditions are favorable, and consumers have strong preference for ecological products. The prices of the two products increase with an increase in γ , and when $c_G + \alpha + \tau - c_E + \beta < \frac{\tau(4-\gamma^2)}{2-\gamma^2+\gamma}$, the price of ecological products is higher than that of general products.

Remarks: From the above, we deduce two products of the same kind and different quality, where, from Eq. (7) ($p_G^{*,1} - p_E^{*,1}$), the price of general products is lower than that of ecological products when $c_G + \alpha + \tau - c_E + \beta < \frac{\tau(4-\gamma^2)}{2-\gamma^2+\gamma}$. This requires that the difference between the production cost of general products with negative externalities to the environment and the marginal cost of ecological products be small, even though the latter has a higher cost than the former. In this situation, the profit of the ecological firm is higher than that of the general firm. This is because the production cost greatly determines the product price and thus affects the profit.

However, from Eq. (8), we can obtain $\frac{\partial p_G^{*,1}}{\partial \gamma} > 0$, $\frac{\partial p_E^{*,1}}{\partial \gamma} > 0$; it is worth noting that the profit of the ecological firm is negative ($\pi_E^{*,1} < 0$), indicating that the ecological firm has no dominant market position in synchronous output competition, and a cost disadvantage encourages the premium behavior of the general firm.

In addition, for ecological products, consumer recognition is not high, and the price is sticky with less fluctuation. On the contrary, Wang & Ng [45] found that a difficulty in consumer recognition results in a new retail firm occupying a larger market share and possibly obtaining higher profits. Notably, the model in this study emphasizes the impact of commodity externalities on pricing. Due to the existence of taxes, general firms usually incur higher production costs and then set higher

prices to pass on the costs to consumers and to ensure profitability.

Interestingly, when market consumption cannot reflect the positive effect of ecological products, consumer utility will reach a maximum. This is different from the common belief that the same kinds of high-quality products can improve the situation of consumers. When faced with the choice of two kinds of goods, consumers are limited by their income levels and fixed cognition, and they will choose familiar traditional products instead.

Dynamic Game of Complete Information

Case of Follower

Under normal conditions, a general firm is the forerunner in the market, and an ecological firm is the follower. The general firm, being in the lead position, makes decisions based on the actions of the ecological firm. The response function of the ecological firm is: $q_E = \frac{A + \gamma q_G - c_E + \beta}{2}$. The general firm's profit maximization problem can be expressed by:

$$\pi_G^{2,1} = \left(A - q_G - \tau + \gamma \frac{A + \gamma q_G - c_E + \beta}{2} \right) q_G - c_G q_G - \alpha q_G \quad (9)$$

$$\frac{\partial \pi_G^{2,1}}{\partial q_G} = A - 2q_G - \tau + \frac{\gamma}{2}A + \gamma^2 q_G - \frac{\gamma}{2}(c_E - \beta) - c_G - \alpha = 0 \quad (10)$$

Then the equilibrium output of the general firm can be obtained by:

$$q_G^{*,2,1} = \frac{(2+\gamma)A - 2(c_G + \alpha + \tau) - \gamma(c_E - \beta)}{4 - 2\gamma^2} \quad (11)$$

Substituting Eq. (11) into Eq. (5) obtains the equilibrium outputs of the ecological firm:

$$q_E^{*,2,1} = \frac{(4-\gamma^2+2\gamma)A - 2\gamma(c_G + \alpha + \tau) - (4-\gamma^2)(c_E - \beta)}{8 - 4\gamma^2} \quad (12)$$

By substituting Eq. (11) and Eq. (12) into Eq. (2), we can obtain the equilibrium prices of the two products in this dynamic game with complete information:

$$\begin{aligned} p_G^{*,2,1} &= \frac{(4 - \gamma^3 - 2\gamma^2 + 2\gamma)A + (4 - 2\gamma^2)(c_G + \alpha + \tau) + (\gamma^3 - 2\gamma)(c_E - \beta)}{8 - 4\gamma^2} - \tau \\ p_E^{*,2,1} &= \frac{(4 - \gamma^2 + 2\gamma)A - 2\gamma(c_G + \alpha + \tau) + (4 - 3\gamma^2)(c_E - \beta)}{8 - 4\gamma^2} \end{aligned} \quad (13)$$

and

$$\begin{aligned} \frac{\partial p_G^{*,2,1}}{\partial \gamma} &= \frac{(4 + \gamma^4 - 4\gamma^2)A - (4 + 3\gamma^4 - 2\gamma^3 + \gamma^2)(c_E - \beta)}{(4 - 2\gamma^2)^2} > 0 \\ \frac{\partial p_E^{*,2,1}}{\partial \gamma} &= \frac{2(2 + \gamma^2 + 2\gamma)A - 2(2 - \gamma^2 + 2\gamma)(c_G + \alpha + \tau) - 4\gamma(c_E - \beta)}{(4 - 2\gamma^2)^2} > 0 \end{aligned} \quad (14)$$

Case of Forerunner

Moreover, high-quality products of the same kind are often developed depending on the original products on the market. In this case, the general firm makes the first decision; as a new entrant to the market, the ecological firm knows the reaction behavior of the general firm.

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